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# Modelling Volatility Spillovers for Bio-ethanol, Sugarcane and Corn

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## Abstract

The recent and rapidly growing interest in biofuel as a green energy source has raised concerns about its impact on the prices, returns and volatility of related agricultural commodities. Analyzing the spillover effects on agricultural commodities and biofuel helps commodity suppliers hedge their portfolios, and manage the risk and co-risk of their biofuel and agricultural commodities. There have been many papers concerned with analyzing crude oil and agricultural commodities separately. The purpose of this paper is to examine the volatility spillovers for spot and futures returns on bio-ethanol and related agricultural commodities, specifically corn and sugarcane, using the multivariate diagonal BEKK conditional volatility model. The daily data used are from 31 October 2005 to 14 January 2015. The empirical results show that in 2 of 6 cases for the spot market, there were significant negative co-volatility spillover effects, specifically corn on subsequent sugarcane co-volatility with corn, and sugarcane on subsequent corn co-volatility with sugarcane. In the other 4 cases, there are no significant co-volatility spillover effects. There are significant positive co-volatility spillover effects in all 6 cases, namely between corn and sugarcane, corn and ethanol, and sugarcane and ethanol, and vice-versa, for each of the three pairs of commodities. It is clear that the futures prices of bio-ethanol and the two agricultural commodities, corn and sugarcane, have stronger co-volatility spillovers than their spot price counterparts. These empirical results suggest that the bio-ethanol and agricultural commodities should be considered as viable futures products in financial portfolios for risk management.

**Keywords** Biofuel, spot prices, futures prices, returns, volatility, risk, co-risk, bio-ethanol, corn, sugarcane, diagonal BEKK model, co-volatility spillover effects, hedging, risk management

**JL Classification** C32, C58, G13, G15, Q14, Q42.

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## Abstract

The recent and rapidly growing interest in biofuel as a green energy source has raised concerns about its impact on the prices, returns and volatility of related agricultural commodities. Analyzing the spillover effects on agricultural commodities and biofuel helps commodity suppliers hedge their portfolios, and manage the risk and co-risk of their biofuel and agricultural commodities. There have been many papers concerned with analyzing crude oil and agricultural commodities separately. The purpose of this paper is to examine the volatility spillovers for spot and futures returns on bio-ethanol and related agricultural commodities, specifically corn and sugarcane, using the multivariate diagonal BEKK conditional volatility model. The daily data used are from 31 October 2005 to 14 January 2015. The empirical results show that in 2 of 6 cases for the spot market, there were significant negative co-volatility spillover effects, specifically corn on subsequent sugarcane co-volatility with corn, and sugarcane on subsequent corn co-volatility with sugarcane. In the other 4 cases, there are no significant co-volatility spillover effects. There are significant positive co-volatility spillover effects in all 6 cases, namely between corn and sugarcane, corn and ethanol, and sugarcane and ethanol, and vice-versa, for each of the three pairs of commodities. It is clear that the futures prices of bio-ethanol and the two agricultural commodities, corn and sugarcane, have stronger co-volatility spillovers than their spot price counterparts. These empirical results suggest that the bio-ethanol and agricultural commodities should be considered as viable futures products in financial portfolios for risk management.

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## **1. Introduction**

Following the Industrial Revolution, as industries rapidly developed all over the world, energy resources began to be used in increasingly large amounts, and oil stocks gradually declined. As the usage and exploitation of the world's oil accelerated, the U.S. Energy Information Administration (EIA) stated that the supply of oil was insufficient to meet demand, and because of speculation and the need to tap into oil reserves, the price of oil became increasingly unstable.

During the First World War, due to the shortage of oil, motor vehicles began to use a mixture of ethanol and gasoline as fuel. As the world subsequently experienced a succession of oil crises, there were dramatic fluctuations in oil prices. For example, in 1973 due to the war in the Middle East, the Organization of the Petroleum Exporting Countries (OPEC) imposed an embargo on exports of oil which led to the First Oil Crisis, during which time the price of crude oil rose from less than US\$3 per barrel to nearly US\$12. In addition, following the outbreak of the Iran-Iraq war in 1979, there was a significant decline in the amount of oil produced, which resulted in the Second Oil Crisis, during which oil prices rose from US\$15 a barrel to nearly US\$39.

Furthermore, excessive use of fossil energy also contributed to global warming and greenhouse gas emissions, with the result that a meeting of the United Nations Framework Convention on Climate Change was convened in Kyoto, Japan in December 1997, at which member countries unanimously agreed to draw up the "Kyoto Protocol". Each country was invited to sign the Protocol between 16 March 1998 and 15 March 1999 in order that, through the implementation of this Agreement, each country's

emissions of greenhouse gases would be reduced. Many countries began to implement policies in response, with the use of biomass energy being an important development. According to EIA data, between 2002 and 2013, biomass energy production grew by more than 60% in the USA, with the main source of this growth being the production of ethanol. Some 60% of the biomass energy crops grown were able to be converted from the original raw materials into biomass fuels. Currently most of this biomass energy is blended with gasoline or diesel and used as fuel in motor vehicles (see Figure 1).

This paper broadly divides biomass energy according to how it is used after production into two categories, namely bio-ethanol and bio-diesel. Bio-ethanol can be blended with gasoline to be used as fuel, and its main sources are corn, cane sugar and sugar beet. Bio-diesel can be blended with diesel fuel, and its main sources are soybeans, palm oil and rapeseed. The USA mainly produces corn and soybeans, while Brazil mainly produces sugar cane, corn and soybeans. The rapeseed used in the manufacture of bio-diesel is mostly grown in Europe, while South-East Asia mainly produces palm oil. From the countries in which these crops are produced, we can see the countries in which the major bio-fuels are manufactured. The USA and Brazil mainly manufacture bio-ethanol, while Europe and South-East Asia concentrate on bio-diesel.

In addition to the agricultural products used in the past to manufacture bio-fuels, in recent years many scholars have begun to study the use of algae as a biomass energy raw material. Different kinds of algae can be used for different purposes. The polysaccharides found in large seaweeds, such as asparagus, ulva and sargassum, can be used to refine ethanol, and micro-algae, such as green algae and diatoms, which are

higher in fats than other energy crops, can also be used as raw materials for bio-diesel (see Figure 2).

Although the USA is the major producer of corn, about 55% to 65% of the corn produced is used as feed, with less than 10% being used as food for human consumption. For this reason, rising corn prices have caused the cost of feeding livestock to increase, with the result that budgets for the costs of technology have been impacted. In addition, impacted by the increased production of corn alcohol, many regions have begun to plant bean crops used as biofuels, hence the yield and price volatility of corn have caused the prices of other crops to become increasingly unstable (Wisner, 2008).

According to the most recent research report prepared by the Renewable Fuels Association (RFA), the increased prices of corn have compensated farm production costs, which has resulted in the federal government reducing its related subsidies. However, the report also points out that the corn used to produce ethanol and the sweet corn needed to supply food for human consumption are different, so that the production of bio-ethanol will not crowd out the quantity of food produced, and will not conflict with food security. Regardless of whether traditional energy crops constitute a threat to either food or land, with the development of biomass energy, in the future more diversified production methods are bound to develop, and new crops, some of which have been mentioned above, will be developed to produce bio-fuels.

Figure 3 shows that from 1980 to 2007, the trends in the proportion of corn used to produce bio-ethanol and corn prices, as the quantity of ethanol produced has increased, corn prices have also rapidly increased. Figure 4 shows that from 1991 to 2012 the

prices of ethanol-related agricultural products, such as corn and sugar cane have, for the most part, remained highly correlated.

In order to manage the environment, at a sustainable level, large numbers of countries around the world are actively promoting the use of biomass energy, and the development of biomass energy is becoming increasingly popular. The primary crops used to produce biomass energy crops are corn and sugarcane, which are mostly used in the production of ethanol, while the main crops used in the production of diesel are beans and rapeseed. In both the spot and futures markets, the price volatility of a target crop used in the production of any kind of biomass energy is likely to increase the volatility in the prices of products involving other crops.

Crop producers may, by means of the price transmission of biomass energy and agricultural crops, as well as the direction in which the returns spillover effects are transmitted, improve the risk management of their portfolios. At the same time, through the risk spillover effects between different agricultural products and biofuels, that is, through the interactions in terms of the fluctuations in risk between different target crops, the volatility and risk of future losses can be reduced.

The concept of risk was proposed as early as 1895 by the American scholar John Haynes, who classified and analyzed different types of risk. Spillover risk, also called transmission risk, refers to a situation that occurs in the short term. When a commodity experiences shocks, resulting in the fluctuations in the combined returns on products changing in either the same or opposite direction, investors can use the positive and negative relationships in the observed risk spillover effects to determine the direction of

the impact of the returns between the different commodities. Thus, they can examine the increases or decreases in the overall risk of their portfolio of commodities. It can then be decided whether the different products can serve as assets within the investment portfolio in order to reduce the portfolio risk. For this reason, producers and managers of agricultural crops need to understand the price volatility of renewable energy crop products and the risk spillover effects of biomass energy, and thereby pursue an effective risk management strategy.

Numerous papers in financial econometrics have proposed univariate conditional risk volatility models, such as the ARCH model of Engle (1982), and GARCH model of Bollerslev (1986), from which related conditional heteroskedastic models that capture the volatility of asset returns have been subsequently derived, such as the threshold TGARCH (or GJR) and EGARCH models (Glosten et al, 1993; McAleer et al, 2008; McAleer, 2014; McAleer and Hafner, 2014; Martinet and McAleer, 2015; Nelson, 1990, 1991; Tsay, 1987).

Using univariate conditional volatility models, Lence and Hayes (2002) examined crude oil, bio-fuel and energy policy, Jin and Frechette (2004) used long memory models, and Egelkraut et al. (2007) examined spillovers between spot and derivatives returns (although this can be problematic using univariate models as estimation is generally not efficient). There seems to have been little or no analysis of asymmetry or leverage in differentiating the effects of positive and negative shocks of equal magnitude on subsequent volatility.

However, individually measuring the risk for futures products in the market cannot

clarify the interdependence between products and their related strengths in current international markets. Therefore, financial econometricians have developed different multivariate risk volatility models, such as the BEKK (Engle and Kroner, 1995), DCC (Engle, 2002) and VARMA-GARCH (Ling and McAleer, 2003) models, in which they discuss the risks transmitted between different assets, also referred to as the risk spillover effects. In recent years, econometricians have gone further to discuss the lack of different statistical properties in multivariate risk volatility models, in the hope that they can more accurately capture the risk transmission effects among assets (Bollerslev, 1990; Bollerslev et al., 1988; Engle, 2002; Hafner and McAleer, 2014; Jeantheau, 1998; Ling and McAleer, 2003; McAleer et al., 2009; Tse and Tsui, 2002).

Volatility spillovers using multivariate models have been considered by Cesar and Marco (2012) and Sendhil et al. (2013), while the BEKK model was used in Trujillo-Barrera et al. (2012), the DCC model was estimated in Cabrera and Schulz (2013), and the CCC, VARMA-GARCH, DCC and BEKK models were analyzed for crude oil spot and futures returns in Chang et al. (2011).

Most previous studies on biomass energy have concentrated on researching the markets for bio-diesel crops, or on discussing the spillover effects among the food crop markets. Relatively few studies have focused on discussing bio-ethanol and the risk transmitted among related crops. In discussing the development of biomass energy, bio-ethanol and bio-diesel both have very important roles to play.

This paper focuses on bio-ethanol and the relevant agricultural products used in the production of bio-ethanol, and will analyze the risk spillover effects for the spot and

futures returns on bio-ethanol, corn and sugar cane, so that the results might serve as a useful reference for policymakers, market investors and crop producers in the optimal management of risk.

The remainder of the paper is as follows. The literature on price transmission and volatility risk spillovers is reviewed in Section 2. In Section 3, we introduce the model specifications. A description of the sample and variables follows in Section 4, followed by the empirical results in Section 5. Some concluding remarks are given in Section 6.

## **2. Literature on Price Transmission and Risk Spillovers**

Past studies on the price transmission of agricultural crops have by and large, in accordance with the efficient markets hypothesis, discussed price transmission and price discovery. Revoredo-Giha and Zuppiroli (2012) discussed the price efficiency in the European and US wheat futures markets, the London International Financial Futures and Options Exchange (LIFFE), the Marché à Terme International de France (MATIF), and the Chicago Mercantile Exchange Group (CBOT). They also calculated wheat futures and their corresponding wheat spot market prices, as well as the hedge ratios for East Anglia (UK), Rouen (France), Bologna (Italy) and Chicago (USA). The authors discovered that the MATIF market was more efficient than the other two futures markets. At the same time, regardless of whether the European or US markets were considered, wheat futures and spot prices were all significantly correlated, indicating that hedging efficiency existed in both the US and European markets.

Sendhil et al. (2013) studied different futures contracts for wheat, chickpea, corn

and barley in Indian markets, and examined whether price transmission and price disclosure existed among spot agricultural markets, using VECM and SUM to measure the price transmission and disclosure effects, respectively. From the results of the VECM, they found that the speeds of adjustment of the spot prices of chickpea and wheat were more rapid than those of the corresponding futures prices, whereas the speed of adjustment of the futures prices for corn was more rapid than that for the corresponding spot prices. The results of SUM indicated that there existed a price disclosure effect in both the spot and futures prices of corn and wheat, and that this price disclosure effect was more significant than in the markets for chickpea and wheat.

In addition to examining the price transmission relationships among agricultural products, Chang et al. (2012) used the M-TAR (Momentum-Threshold Autoregressive) model and VECM to analyze the price transmission effects for bio-energy in different areas, as well as the speed of the price adjustment of three kinds of energy crops, namely corn, soybeans and sugar, and the price transmission effects between biomass energy and energy crops. It was found that bio-ethanol exhibited different speeds of price adjustment in different regions, implying that there exist opportunities to engage in arbitrage and price hedging. The price adjustment factor in relation to corn was the most significant, while the price adjustment factor in relation to sugar was the weakest. Bio-ethanol futures and agricultural products, due to their different speeds of price adjustment, could be used as a hedge against prices in food commodity markets.

A number of related studies in the literature that used the VECM to measure the price transmission effects between energy products and agricultural crops also found

evidence of the existence of a price transmission relationship (see, among others, Trujillo-Barrera et al., 2012; Cabrera and Schulz, 2013; Zhang et al., 2009; Zhang et al., 2014).

Zhao and Goodwin (2011) used Black's (1976) model to calculate the implied risk for corn and soybeans, and the VAR model to analyze the implied risk transmission relationship between corn and soybeans. Their results indicated that there was a risk spillover effect between corn and soybeans, but not the reverse. In addition, the authors used the threshold model to analyze the risk spillover effects between different time periods and found that, when the risk volatility of soybeans was high, soybeans exhibited a risk spillover effect in relation to corn; when the risk volatility of corn was high, soybeans exhibited a positive risk transmission relationship with corn; and when the risk volatility of corn was low, this risk transmission exhibited a negative relationship. The authors also compared the risk spillover effects estimated with the BEKK model. The results indicated that corn exhibited a risk spillover effect in relation to soybeans, and that the risk spillover effect for soybeans in relation to corn was significant.

Nazlioglu et al. (2013) used the causality in variance approach proposed by Hafner and Herwartz (2006) to analyze the spot price risk spillover effects between crude oil and corn, sugar, soybeans and wheat, both before and after the food price crisis of 2005. Their results indicated that prior to the outbreak of the food price crisis, only wheat exhibited a significant risk spillover effect in relation to crude oil, there being no such effect for the other crops. Moreover, there was no evidence of a risk spillover effect for

petroleum in relation to these four agricultural crops.

However, after the food crisis occurred, apart from in the case of petroleum in relation to sugar, there was evidence of a significant risk transmission effect for petroleum in relation to all other products. As the volatility of petroleum prices became more pronounced, which led more countries to develop biomass energy products as alternatives to standard energy sources, the price volatilities of related agricultural products became higher than they had been in the past. Moreover, the prices of these products over time became more highly correlated with the price of petroleum. Previous studies that have discussed the risk spillover effects among markets for bio-ethanol, fossil fuels and agricultural products are mostly concentrated on the USA, Brazil and Europe (see, among others, Serra, 2011, 2012; Serra et al., 2011; Serra and Gil 2013).

Multivariate GARCH models used to measure the risk transmission or risk spillover effects between different commodities may be divided into two types. The first approach uses conditional covariances to explain the risk spillover effects between different commodities, such as the VECM and BEKK models. A second approach uses conditional correlations to analyze the correlations in the fluctuations between different commodities, such as the CCC (Bollerslev, 1990) and DCC (Engle, 2002) models. Regardless of whether the focus of the research is on futures and spot markets for agricultural products, between different agricultural products, or between energy and agricultural products, these models are very important when it comes to examining the roles played by risk transmission effects in reducing portfolio risk. The following gives a brief review.

Trujillo-Barrera et al. (2012) used the Full BEKK model, that is, with no restrictions on the parameters in the conditional covariance matrix, to analyze the risk spillover effects for US crude oil, bio-ethanol and corn futures, and to measure the intensity of the risk transmission of crude oil futures prices on corn and bio-ethanol. The empirical results indicated that corn had a significant risk spillover effect on bio-ethanol, but not the reverse. There was a relatively high degree of intensity in terms of the spillover effects of crude oil on bio-ethanol.

Zhang et al. (2009) also used the Full BEKK model to analyze the risk spillover effects between ethanol and agricultural products (namely, corn and soybeans), but the analysis was divided into two different periods, namely the early ethanol development period (1989-1999) and the later period (2000-2007). The results indicated that no significant risk transmission relationship was found to exist between ethanol and corn and soybeans in the development period. It was only in the late ethanol development period that there was evidence of a risk spillover effect from soybeans to ethanol.

Cabrera and Schulz (2013) used the GARCH and DCC multivariate volatility model to analyze the risk spillover effects among crude oil, bio-diesel and rapeseed. The empirical results showed that there was a significant risk spillover effect between crude oil and rapeseed, but the risk spillover effect between bio-diesel and rapeseed was not significant. The authors argued that crude oil and rapeseed were globally traded commodities, whereas trade in bio-diesel tended to be limited to the European region. Therefore, there was no clear evidence of risk spillover effects between bio-diesel and the other two commodities.

Chang et al. (2011) analyzed the risk transmission effects based on spot and futures market data for the two major crude oil markets, namely Brent and WTI. They compared the CCC, VARMA-GARCH, DCC, Full BEKK and Diagonal BEKK models, and found that, regardless of which model was used, the holding ratios for Brent crude oil futures always needed to be greater than the corresponding ratios in the spot market. However, in the WTI crude oil market, the results of the CCC and VARMA-GARCH models indicated that the spot market holding ratios needed to be greater than the corresponding ratios in the futures market.

In contrast, when the dynamic DCC and BEKK models were used, it was found that the spot market holding ratios should be larger than those in the futures market. In addition, by using hedging effectiveness to select the best model, the results indicated that the Diagonal BEKK model had the best hedging effectiveness, and was the best model used to calculate the asset portfolio. However, the BEKK model had the lowest hedging effectiveness value, and was therefore the least suitable model.

### **3. Model Specifications**

In order to investigate volatility spillover effects empirically, the diagonal BEKK model will be used to examine volatility spillover effects (see McAleer et al. (2008) for an explanation of the regularity conditions and asymptotic properties of alternative BEKK models, including the scalar, diagonal, triangular, Hadamard and Full BEKK specifications). The full BEKK model, together with the conditional mean equation for financial returns, is given as:

$$Y_t = A_0 + A_1 Y_{t-1} + \varepsilon_t \quad (1)$$

$$H_t = CC' + A\varepsilon_{t-1}\varepsilon'_{t-1}A' + BH_{t-1}B' \quad (2)$$

where  $Y_t$  denotes returns,  $\varepsilon_t$  is the returns shock,  $H_t$  is the conditional covariance matrix of the returns shocks, and  $H$ ,  $C$ ,  $A$  and  $B$  are  $m \times m$  matrices. As the full BEKK model in equation (2) is not derived from a known stochastic process, it has no regularity conditions, except by assumption, and hence also has no asymptotic properties. Moreover, estimation of the full BEKK model involves  $3m(m+1)/2$  parameters. As the number of parameters increases, convergence of the estimation algorithm becomes problematic because of the associated “curse of dimensionality”. Convergence of the estimation algorithm is more likely when the number of commodities is less than 4, though this is nevertheless problematic in terms of interpretation.

A special case of Full BEKK is the Diagonal BEKK model, which can be derived from an underlying stochastic process when the matrices  $A$  and  $B$  are diagonal or scalar matrices, with  $a_{ii} > 0$  for all  $i = 1, \dots, m$  and  $|b_{jj}| < 1$  for all  $j = 1, \dots, m$ . The Quasi-Maximum Likelihood Estimates (QMLE) of the parameters of the Diagonal BEKK model can be shown to be consistent and asymptotically normal, so that standard statistical inference is valid. The Diagonal BEKK model is given as equation (2), where the matrices  $A$  and  $B$  are given as:

$$A = \begin{bmatrix} a_{11} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & a_{mm} \end{bmatrix}, B = \begin{bmatrix} b_{11} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & b_{mm} \end{bmatrix}$$

The Diagonal BEKK model permits a test of Co-volatility Spillover effects, which is the effect of a shock in commodity  $j$  at  $t-1$  on the subsequent co-volatility between  $j$  and another commodity at  $t$ . Given the nature of the Diagonal BEKK model, the subsequent co-volatility must be between commodities  $j$  and  $i$  at time  $t$ . This leads to the definition of a Co-volatility Spillover Effect as:

**Definition:**  $\frac{\partial H_{ij,t}}{\partial \varepsilon_{j,t-1}} = a_{ii} \times a_{jj} \times \varepsilon_{i,t-1}, i \neq j.$

As  $a_{ii} > 0$  for all  $i$ , a test of the co-volatility spillover effect is given as:

$$H_0: a_{ii}a_{jj} = 0,$$

which is a test of the significance of the estimate of  $a_{ii}a_{jj}$  in the following co-volatility spillover effect, as  $\varepsilon_{i,t-1} \neq 0$ :

$$\frac{\partial H_{ij,t}}{\partial \varepsilon_{j,t-1}} = a_{ii}a_{jj}\varepsilon_{i,t-1}, i \neq j.$$

If  $H_0$  is rejected, there is a spillover from the returns shock of commodity  $j$  at  $t-1$  to the co-volatility between commodities  $i$  and  $j$  at  $t$  that depends only on the returns shock of commodity  $i$  at  $t-1$ . It should be emphasized that the returns shock of commodity  $j$  at  $t-1$  does not affect the co-volatility spillover of commodity  $j$  on the co-volatility between commodities  $i$  and  $j$  at  $t$ . Moreover, spillovers can and do vary for each observation  $t-1$ .

#### **4. Data and Variables**

This paper uses daily time series data on the spot prices and closing futures prices of bio-ethanol and two agricultural commodities, namely corn and sugar, in the empirical analysis. The sample covers the period 31 October 2005 to 14 January 2015. The length of this period was dictated by the availability of data on ethanol spot and futures trading in the USA.

The data on corn and sugarcane spots are sourced from the United States Department of Agriculture (USDA). The corn spot is corn number 2 yellow (class CORNUS2), and is expressed in US cents per bushel. The sugar spot is raw cane sugar, world (class SUGCNRW), and is expressed in US cents per pound. The bio-ethanol spot is sourced from Thomson Reuters, and is expressed in US dollars per gallon. Data on corn closing futures prices are sourced from Datastream for the US market.

The corn futures class is CC, traded at the Chicago Board of Trade (CBOT), and is expressed in US cents per bushel. Sugar futures is given as sugar # 11 (class NSB), is expressed in US cents per pound, traded at the Coffee, Sugar & Cocoa Exchange Inc (CSCE). The bio-ethanol futures price is sourced from Thompson Reuters and is expressed in US dollars per gallon. Its class is CZE, and is expressed in US dollars per gallon, traded on eCBOT.

The endogenous variables used in the paper is the daily return rate, where the rate of return is obtained as the natural logarithm of the daily price data, and subtracting the natural logarithms of the daily price data for two consecutive days from each other, and

multiplying by 100.  $Corn_{sr}$ ,  $Sugar_{sr}$ , and  $Ethanol_{sr}$  represent the spot returns for corn, sugarcane, and bio-ethanol, and  $Corn_{fr}$ ,  $Sugar_{fr}$ ,  $Ethanol_{fr}$  represent the futures returns of corn, sugarcane, and bio-ethanol, respectively. The variable definitions are given in Table 1.

**[Insert Table 1 here]**

The descriptive statistics for the endogenous returns of the spot and futures for bio-ethanol and the two agricultural commodities, corn and sugarcane, are given in Table 2. The highest standard deviation for the futures market over the sample period is for bio-ethanol, followed by sugarcane, while the highest standard deviation for the spot market over the sample period is for corn.

The returns have different degrees of skewness. Interestingly, virtually all the returns are skewed to the left, indicating that these futures series have longer left tails (extreme losses) than right tails (extreme gains), except for bio-ethanol spot and sugar futures returns, which are skewed to the right. This stylized fact should be of interest to participants in commodity markets. All of the price distributions have kurtosis that is significantly higher than 3, implying that higher probabilities of extreme market movements in either direction (gains or losses) occur in these futures markets, with greater frequency in practice than would be predicted by the normal distribution. In the spot market, the highest kurtosis is for ethanol spot, followed by sugarcane and corn, while in the futures market, the highest is for sugarcane, followed by bio-ethanol and corn. The Jarque-Bera Lagrange multiplier statistics confirm non-normal distributions

in all the return series.

As shown in Figure 5, the volatility of returns for spot and futures of bio-ethanol and the two agricultural commodities display the phenomenon of volatility clustering.

**[Insert Figure 5 and Table 2 here]**

The unit root tests for both endogenous and exogenous variables are summarized in Table 3. The Augmented Dickey-Fuller (ADF) and Phillips-Perron (PP) tests were used to test for unit roots in the individual returns series. The ADF test accommodates serial correlation by specifying explicitly the structure of serial correlation in the errors. The non-parametric PP test allows fairly mild assumptions that do not assume a specific type of serial correlation and heteroskedasticity in the disturbances, and can have higher power than the ADF test under a wide range of circumstances. The null hypothesis of the ADF and PP tests is that the series have a unit root (for further details, see Dickey and Fuller, 1979; Phillips and Perron, 1988). In Table 3, based on the ADF and PP test results, the large negative values in all cases indicate rejection of the null hypothesis of unit roots at the 1% level of significance. Therefore, all the returns series are stationary.

**[Insert Table 3 here]**

## **5. Empirical Results for Co-volatility Spillover Effects**

### **5.1 Testing Co-volatility Spillover Effects**

It is possible to check directly the Co-volatility Spillover effects through testing the significance of the estimates of the matrix  $A$  in the Diagonal BEKK model. If the null hypothesis  $H_0$  is rejected, there will be spillovers from the returns shock of commodity  $j$  at  $t-1$  to the co-volatility between commodities  $i$  and  $j$  at  $t$  that depends only on the returns shock of commodity  $i$  at  $t-1$ .

Tables 4-6 show the empirical results of spot markets for the VAR(1,1) - multivariate diagonal BEKK(1,1) model, and the results of testing the Co-volatility Spillover effects from the significance of the estimates of the matrix  $A$  in the Diagonal BEKK model. Estimation of the model in equations (1) and (2) by QMLE are undertaken using both the EViews and RATS econometric software packages for comparison. Table 4 reports the estimates for corn and bio-ethanol, Table 5 reports the results for sugarcane and bio-ethanol, and Table 6 reports the estimates for corn, sugar, and ethanol.

From the estimates of matrix  $A$  of the Diagonal BEKK model in Table 4, both coefficients are statistical significant at the 1% level, which shows spillovers from corn on subsequent bio-ethanol co-volatility with corn, and bio-ethanol on subsequent corn co-volatility with bio-ethanol. However, Table 5 shows that that not all the estimates in  $A$  are significantly different from zero: there is a spillover effect from the returns shock of sugar at  $t-1$  to the co-volatility between sugar and ethanol, but no significant effect from the returns shock of ethanol at  $t-1$  to the co-volatility between sugar and ethanol.

If we add three commodities to the Diagonal BEKK model, we can see the empirical results more clearly. As shown in the estimates of the matrix  $A$  in Table 6,

there are a significant co-volatility spillover effects, particularly corn on subsequent sugarcane co-volatility with corn, and sugarcane on subsequent corn co-volatility with sugarcane.

Table 7 - 9 show the results of the futures markets for VAR(1,1) - Diagonal BEKK (1,1) model, and the results of testing the co-volatility spillover effects from the significance of the estimates of  $A$  in the Diagonal BEKK model. Table 7 reports the estimates for corn and bio-ethanol, Table 8 reports the results for sugarcane and bio-ethanol, and Table 9 reports the estimates for corn, sugar, and ethanol.

In Table 7, both coefficients in  $A$  are statistically significant at the 1% level, which indicates corn on subsequent bio-ethanol co-volatility with corn, and bio-ethanol on subsequent corn co-volatility with bio-ethanol. We also found spillover effects in the futures market of sugarcane and bio-ethanol as the estimates of  $A$  in Table 8 show significant effects of sugarcane on subsequent bio-ethanol co-volatility with sugarcane, and bio-ethanol on subsequent sugarcane co-volatility with bio-ethanol.

In Table 9, as we add three commodities into the Diagonal BEKK system, we can see clearly that there are significant co-volatility spillover effects in all 6 cases, namely between corn and sugarcane, corn and ethanol, and sugarcane and ethanol, and the reverse.

## **5.2 Calculating Co-volatility Spillover Effects**

We use the definition of Co-volatility Spillover Effects in Section 3 to calculate the average Co-volatility Spillover Effects for the three commodities in the spot and futures

markets. Table 10 shows the average of the return shocks for three commodities in the spot and futures market, while Table 11 shows the results of average Co-volatility Spillover Effects. From the second row of Table 11, it was found in 2 of 6 cases that there were significant negative co-volatility spillover effects, specifically corn on subsequent sugarcane co-volatility with corn, and sugarcane on subsequent corn co-volatility with sugarcane. In Tables 4-6, for the other 4 cases, no significant co-volatility spillover effects were evident.

Unlike the case of spot prices, as shown in the third row in Table 11, there are significant positive co-volatility spillover effects in all 6 cases, namely between corn and sugarcane, corn and ethanol, and sugarcane and ethanol, and the reverse. It is clear that the futures prices of bio-ethanol and the two agricultural commodities, corn and sugarcane, have stronger co-volatility spillovers than their spot price counterparts.

## **6. Concluding Remarks**

The purpose of the paper was to examine the volatility spillovers for spot and futures returns on bio-ethanol and related agricultural commodities, namely corn and sugarcane, using the multivariate Diagonal BEKK multivariate conditional volatility model. The daily data used in the empirical analysis are from 31 October 2005 to 14 January 2015.

For the spot market, it was found that in 2 of 6 cases, there were significant negative co-volatility spillover effects, specifically corn on subsequent sugarcane co-volatility with corn, and sugarcane on subsequent corn co-volatility with sugarcane.

In the other 4 cases for the spot market, there were no significant co-volatility spillover effects. For futures markets, unlike the case of the spot markets, there were significant positive co-volatility spillover effects in all 6 cases, namely between corn and sugarcane, corn and ethanol, and sugarcane and ethanol, and the reverse.

It is clear that the futures prices of bio-ethanol and the two agricultural commodities, namely corn and sugarcane, have stronger co-volatility spillovers than their spot price counterparts. These results strongly suggest that bio-ethanol and agricultural commodities should be considered as viable futures products in financial portfolios for optimal risk management and in calculating hedge ratios

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**Table1**  
**Data Sources**

<b>Variable name</b>	<b>Definitions</b>	<b>Transaction market</b>	<b>Description</b>
<b>Corn<sub>sr</sub></b>	Corn spot return	United States Department of Agriculture (USDA)	Corn Number 2 Yellow (US cents per bushel)
<b>Corn<sub>fr</sub></b>	Corn futures return	Chicago Board of Trade (CBOT)	Chicago Board of Trade (CBOT)-Corn (US cents per bushel)
<b>Sugar<sub>sr</sub></b>	Sugar spot return	United States Department of Agriculture (USDA)	Raw Cane Sugar (US cents per Pound)
<b>Sugar<sub>fr</sub></b>	Sugar futures return	Coffee, Sugar & Cocoa Exchange Inc (CSCE)	CSCE-Sugar #11 (US cents per Pound)
<b>Ethanol<sub>sr</sub></b>	Ethanol spot return	Thomson Reuters	Ethanol, Spot Chicago United States (Dollar Per Gallon)
<b>Ethanol<sub>fr</sub></b>	Ethanol futures return	Chicago Board of Trade (CBOT)	ECBOT-Ethanol

**Table 2**  
**Descriptive Statistics**

<b>Returns</b>	<b>Mean</b>	<b>SD</b>	<b>Max</b>	<b>Min</b>	<b>Skewness</b>	<b>Kurtosis</b>	<b>Jarque-Bera</b>
<b>Corn<sub>sr</sub></b>	0.005	1.661	10.888	-12.307	-0.287	4.704	8796.03
<b>Corn<sub>fr</sub></b>	0.005	1.581	9.801	-24.528	-0.643	14.858	87105.45
<b>Sugar<sub>sr</sub></b>	-0.003	2.321	20.904	-20.097	-0.118	5.644	10666.35
<b>Sugar<sub>fr</sub></b>	0.006	2.892	81.621	-35.390	2.656	81.990	2644229.19
<b>Ethanol<sub>sr</sub></b>	-0.014	3.637	94.039	-79.729	2.341	290.993	8480493.70
<b>Ethanol<sub>fr</sub></b>	-0.027	2.178	9.403	-21.566	-2.115	15.951	26030.49

**Table 3**  
**Unit Root Tests**

<b>Variables</b>	<b>ADF test</b>		
	<b>no trend and intercept</b>	<b>with intercept</b>	<b>with trend and intercept</b>
<b>Corn<sub>sr</sub></b>	-96.112*	-96.108*	-96.103*
<b>Corn<sub>fr</sub></b>	-93.266*	-93.261*	-93.257*
<b>Sugar<sub>sr</sub></b>	-93.491*	-93.486*	-66.833*
<b>Sugar<sub>fr</sub></b>	-74.394*	-74.391*	-74.387*
<b>Ethanol<sub>sr</sub></b>	-24.679*	-24.674*	-24.676*
<b>Ethanol<sub>fr</sub></b>	-43.089*	-43.087*	-43.081*

<b>Variables</b>	<b>PP test</b>		
	<b>no trend and intercept</b>	<b>with intercept</b>	<b>with trend and intercept</b>
<b>Corn<sub>sr</sub></b>	-96.430*	-96.425*	-96.420*
<b>Corn<sub>fr</sub></b>	-93.243*	-93.239*	-93.234*
<b>Sugar<sub>sr</sub></b>	-93.425*	-93.419*	-93.175*
<b>Sugar<sub>fr</sub></b>	-102.251*	-102.247*	-102.241*
<b>Ethanol<sub>sr</sub></b>	-49.528*	-49.518*	-49.517*
<b>Ethanol<sub>fr</sub></b>	-43.108*	-43.104*	-43.098*

**Note:** \* denotes the null hypothesis of a unit root is rejected at the 1% level of significance.

**Table 4**  
**Diagonal BEKK-Spot ( $Corn_{sr}$ ) ( $Ethanol_{sr}$ )**

Mean equation	$Corn_{sr}$	$Ethanol_{sr}$
$Corn_{sr}(-1)$	0.002 (0.021)	0.059* (0.018)
$Ethanol_{sr}(-1)$	-0.015 (0.011)	0.002 (0.116)
C	0.049 (0.039)	0.011 (0.053)

Diagonal BEKK	C	A	B	
$Corn_{sr}$	0.099* (0.016)	0.002 (0.005)	0.222* (0.012)	0.964* (0.004)
$Ethanol_{sr}$		0.086* (0.004)	0.172* (0.002)	0.983* (0.000)
Log-likelihood	-10875.29			
AIC	9.066			

Notes : 1.  $A = \begin{bmatrix} a_{11} & 0 \\ 0 & a_{22} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 \\ 0 & b_{22} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} \\ 0 & c_{22} \end{bmatrix}$

2. Standard errors are given in parentheses, \* significance level 1%.

**3. Substituted Coefficients:**

$$GARCH1 = 0.099 + 0.049 \times RESID1(-1)^2 + 0.929 \times GARCH1(-1)$$

$$GARCH2 = 0.086 + 0.029 \times RESID2(-1)^2 + 0.966 \times GARCH2(-1)$$

$$COV1\_2 = 0.002 + 0.0381 \times RESID1(-1) \times RESID2(-1) + 0.947 \times COV1\_2(-1)$$

**Table 5**  
**Diagonal BEKK-Spot ( $Sugar_{sr}$ ) ( $Ethanol_{sr}$ )**

Mean equation	$Sugar_{sr}$	$Ethanol_{sr}$
$Sugar_{sr}(-1)$	-0.028 (0.027)	0.071*** (0.022)
$Ethanol_{sr}(-1)$	-0.050*** (0.020)	-0.001 (0.362)
C	0.071 (0.054)	0.013 (0.056)

Diagonal BEKK	C	A	B
$Sugar_{sr}$	0.908*** (0.018)	0.106 (0.102)	0.297*** (0.013)
$Ethanol_{sr}$	2.120*** (0.009)	-0.001 (0.591)	0.862*** (0.004)
Log-likelihood	-6479.229		
AIC	8.785		

Notes : 1.  $A = \begin{bmatrix} a_{11} & 0 \\ 0 & a_{22} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 \\ 0 & b_{22} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} \\ 0 & c_{22} \end{bmatrix}$

2. Standard errors are given in parentheses, \* significance level 1%.

3. Substituted Coefficients:

$$GARCH1 = 0.908 + 0.088 \times RESID1(-1)^2 + 0.743 \times GARCH1(-1)$$

$$GARCH2 = 2.120 + 0.000 \times RESID2(-1)^2 + 0.041 \times GARCH2(-1)$$

$$COV1\_2 = 0.106 + 0.256 \times RESID1(-1) \times RESID2(-1) - 0.0002 \times COV1\_2(-1)$$

**Table 6**  
**Diagonal BEKK-Spot ( $Corn_{sr}$ ) ( $Sugar_{sr}$ ) ( $Ethanol_{sr}$ )**

Mean equation	$Corn_{sr}$	$Sugar_{sr}$	$Ethanol_{sr}$
$Corn_{sr}(-1)$	-0.003 (0.025)	0.081** (0.024)	-0.005 (0.026)
$Sugar_{sr}(-1)$	0.007 (0.022)	-0.051* (0.025)	0.073* (0.023)
$Ethanol_{sr}(-1)$	-0.027 (0.029)	-0.051* (0.021)	-0.002 (0.025)
C	0.151** (0.053)	0.074 (0.053)	0.015 (0.055)

Diagonal BEKK	C			A			B		
$Corn_{sr}$	0.422** (0.076)	0.171** (0.045)	0.164 (0.162)	0.224** (0.0256)			0.958** (0.011)		
$Sugar_{sr}$		0.753** (0.029)	0.074 (0.110)		0.248** (0.024)			0.902** (0.008)	
$Ethanol_{sr}$			1.999** (0.013)			-0.001 (0.024)			0.377** (0.014)
Log-likelihood	-9736.477								
AIC	13.208								

Notes : 1.  $A = \begin{bmatrix} a_{11} & 0 & 0 \\ 0 & a_{22} & 0 \\ 0 & 0 & a_{33} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 & 0 \\ 0 & b_{22} & 0 \\ 0 & 0 & b_{33} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ 0 & c_{22} & c_{23} \\ 0 & 0 & c_{33} \end{bmatrix}$

2. Standard errors are given in parentheses, \* significance level 5%, \*\* significance level 1%.

3. Substituted Coefficients:

$GARCH1 = 0.422 + 0.050 \times RESID1(-1)^2 + 0.918 \times GARCH1(-1)$

$GARCH2 = 0.753 + 0.062 \times RESID2(-1)^2 + 0.814 \times GARCH2(-1)$

$GARCH3 = 1.999 + 0.000 \times RESID3(-1)^2 + 0.142 \times GARCH3(-1)$

$COV1\_2 = 0.171 + 0.056 \times RESID1(-1) \times RESID2(-1) + 0.864 \times COV1\_2(-1)$

$COV1\_3 = 0.164 + 0.001 \times RESID1(-1) \times RESID3(-1) + 0.361 \times COV1\_3(-1)$

$COV2\_3 = 0.074 + 0.001 \times RESID2(-1) \times RESID3(-1) + 0.340 \times COV2\_3(-1)$

**Table 7**  
**Diagonal BEKK-Futures ( $Corn_{fr}$ ) ( $Ethanol_{fr}$ )**

Mean equation	$Corn_{fr}$	$Ethanol_{fr}$
$Corn_{fr}(-1)$	0.006 (0.023)	0.022 (0.018)
$Ethanol_{fr}(-1)$	0.048* (0.019)	0.049* (0.022)
C	0.013 (0.039)	-0.037 (0.029)

	C	A	B
$Corn_{fr}$	0.082** (0.010)	0.044** (0.005)	0.205** (0.009)
$Ethanol_{fr}$	0.038** (0.007)	0.327** (0.007)	0.972** (0.002)
Log-likelihood	-9189.522		
AIC	8.0266		

Notes : 1.  $A = \begin{bmatrix} a_{11} & 0 \\ 0 & a_{22} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 \\ 0 & b_{22} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} \\ 0 & c_{22} \end{bmatrix}$

2. Standard errors are given in parentheses, \* significance level 5%, \*\* significance level 1%.

3. Substituted Coefficients:

$$GARCH1 = 0.082 + 0.042 \times RESID1(-1)^2 + 0.945 \times GARCH1(-1)$$

$$GARCH2 = 0.038 + 0.107 \times RESID2(-1)^2 + 0.904 \times GARCH2(-1)$$

$$COV1\_2 = 0.044 + 0.067 \times RESID1(-1) \times RESID2(-1) + 0.924 \times COV1\_2(-1)$$

**Table 8**  
**Diagonal BEKK-Futures ( $Sugar_{fr}$ ) ( $Ethanol_{fr}$ )**

Mean equation			$Sugar_{fr}$			$Ethanol_{fr}$
Sugar <sub>fr</sub> (-1)			0.006			0.029*
			(0.020)			(0.015)
Ethanol <sub>fr</sub> (-1)			0.017			0.051**
			(0.018)			(0.021)
C			-0.042			-0.042
			(0.038)			(0.036)

	C			A			B		
$Sugar_{fr}$	0.025***	0.004			0.199***			0.978***	
	(0.006)	(0.005)			(0.009)			(0.002)	
$Ethanol_{fr}$			0.095***			0.299***			0.949***
			(0.012)			(0.010)			(0.003)
Log-likelihood	-9692.554								
AIC	8.465								

Notes: 1.  $A = \begin{bmatrix} a_{11} & 0 \\ 0 & a_{22} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 \\ 0 & b_{22} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} \\ 0 & c_{22} \end{bmatrix}$

2. Standard errors are given in parentheses, \* significance level 10%, \*\* significance level 5%, \*\*\* significance level 1%.

3. Substituted Coefficients:

$$GARCH1 = 0.025 + 0.040 \times RESID1(-1)^2 + 0.956 \times GARCH1(-1)$$

$$GARCH2 = 0.095 + 0.090 \times RESID2(-1)^2 + 0.900 \times GARCH2(-1)$$

$$COV1\_2 = 0.004 + 0.060 \times RESID1(-1) \times RESID2(-1) + 0.928 \times COV1\_2(-1)$$

**Table 9**  
**Diagonal BEKK-Futures ( $Corn_{fr}$ ) ( $Sugar_{fr}$ ) ( $Ethanol_{fr}$ )**

Mean equation	$Corn_{fr}$	$Sugar_{fr}$	$Ethanol_{fr}$
$Corn_{fr}(-1)$	0.004 (0.023)	-0.001 (0.021)	0.020 (0.020)
$Sugar_{fr}(-1)$	0.017 (0.017)	0.005 (0.019)	0.018 (0.014)
$Ethanol_{fr}(-1)$	0.045* (0.019)	0.014 (0.020)	0.047* (0.022)
C	0.011 (0.039)	-0.035 (0.039)	-0.035 (0.030)

	C	A			B
$Corn_{fr}$	0.080** (0.010)	0.004 (0.003)	0.047** (0.005)	0.187** (0.010)	0.975** (0.002)
$Sugar_{fr}$		0.022** (0.005)	0.002 (0.004)	0.176** (0.008)	0.982** (0.002)
$Ethanol_{fr}$			0.045*** (0.007)	0.323** (0.007)	0.951** (0.002)
Log-likelihood	-14052.30				
AIC	12.278				

**Notes:** 1.  $A = \begin{bmatrix} a_{11} & 0 & 0 \\ 0 & a_{22} & 0 \\ 0 & 0 & a_{33} \end{bmatrix}$ ,  $B = \begin{bmatrix} b_{11} & 0 & 0 \\ 0 & b_{22} & 0 \\ 0 & 0 & b_{33} \end{bmatrix}$ ,  $C = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ 0 & c_{22} & c_{23} \\ 0 & 0 & c_{33} \end{bmatrix}$

2. Standard errors are in the parentheses. \* significance level 5%, \*\* significance level 1%.

3. Substituted Coefficients:

$$GARCH1 = 0.080 + 0.035 \times RESID1(-1)^2 + 0.951 \times GARCH1(-1)$$

$$GARCH2 = 0.022 + 0.031 \times RESID2(-1)^2 + 0.965 \times GARCH2(-1)$$

$$GARCH3 = 0.045 + 0.104 \times RESID3(-1)^2 + 0.904 \times GARCH3(-1)$$

$$COV1\_2 = 0.004 + 0.033 \times RESID1(-1) \times RESID2(-1) + 0.958 \times COV1\_2(-1)$$

$$COV1\_3 = 0.047 + 0.060 \times RESID1(-1) \times RESID3(-1) + 0.927 \times COV1\_3(-1)$$

$$COV2\_3 = 0.002 + 0.057 \times RESID2(-1) \times RESID3(-1) + 0.934 \times COV2\_3(-1)$$

**Table 10**  
**Average Return Shocks**

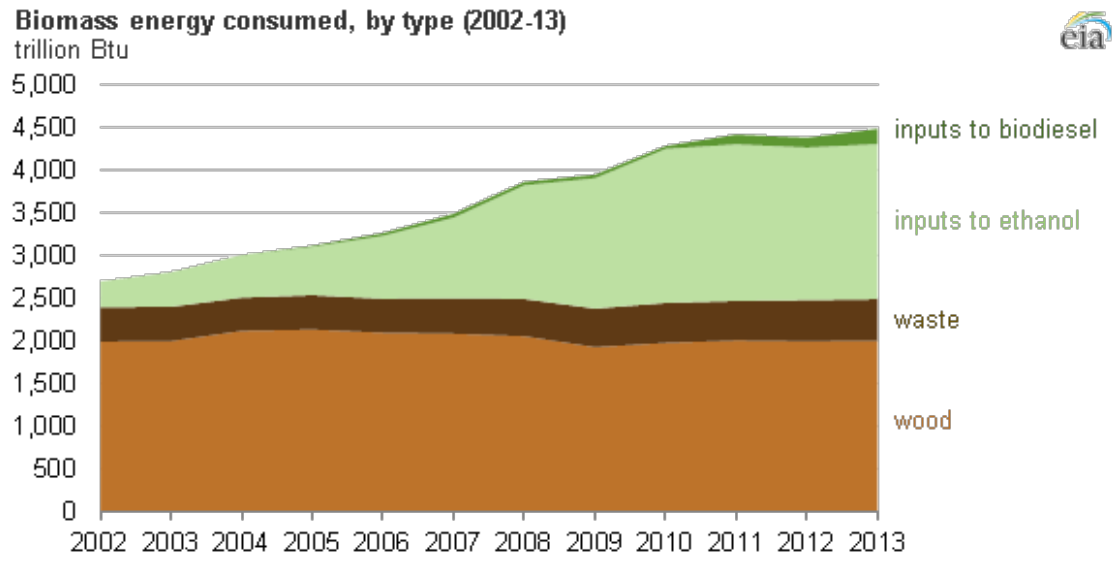
Market	Commodities	Average of return shock
Spot	Corn	-0.064
	Sugarcane	-0.016
	ethanol	0.002
Futures	Corn	0.011
	Sugarcane	0.028
	Ethanol	0.008

**Table 11**  
**Risk Spillovers**

Market	$\left( \frac{\partial H_{ij,t}}{\partial \varepsilon_{j,t-1}} \right)$	Average Co-volatility Spillover
Spot	j=corn, i=sugarcane	-0.0036 (0.224×0.248×(-0.064))
	j=sugarcane, i=corn	-0.0009 (0.224×0.248×(-0.016))
	j=corn, i=ethanol	0
	j=ethanol, i=corn	0
	j=sugarcane, i=ethanol	0
	j=ethanol, i=sugarcane	0
Futures	<b>j=corn, i=sugarcane</b>	<b>0.0009 (0.187×0.176×0.028)</b>
	j=sugarcane, i=corn	0.0004 (0.187×0.176×0.011)
	j=corn, i=ethanol	0.0005 (0.187×0.323×0.008)
	j=ethanol, i=corn	0.0007 (0.187×0.323×0.011)
	j=sugarcane, i=ethanol	0.0005 (0.176×0.323×0.008)
	j=ethanol, i=sugarcane	0.0016 (0.176×0.323×0.028)

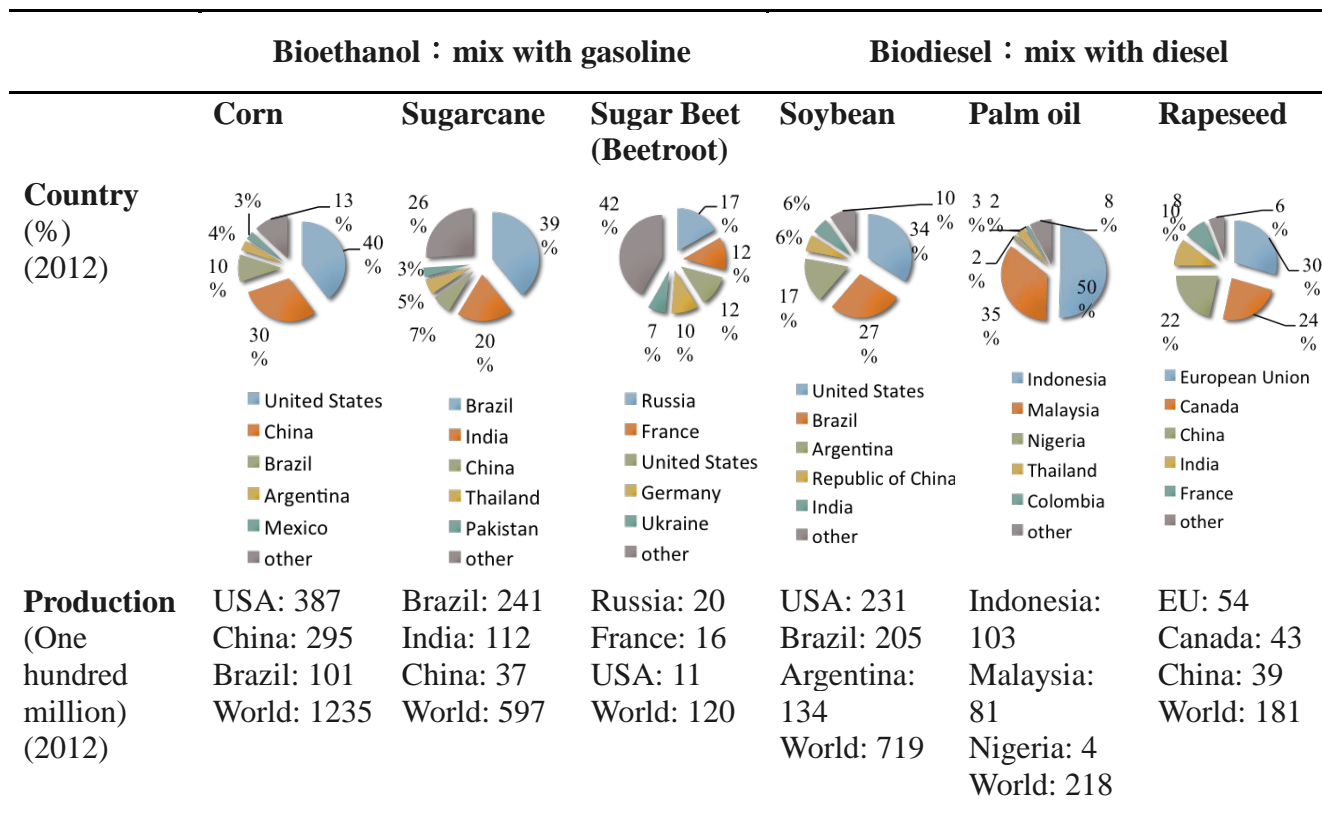
**Note:** Co-volatility Spillover =  $\frac{\partial H_{ij,t}}{\partial \varepsilon_{j,t-1}} = a_{ii} \times a_{jj} \cdot \varepsilon_{i,t-1}$ .

**Figure 1**  
**Use of Biomass Energy in USA**

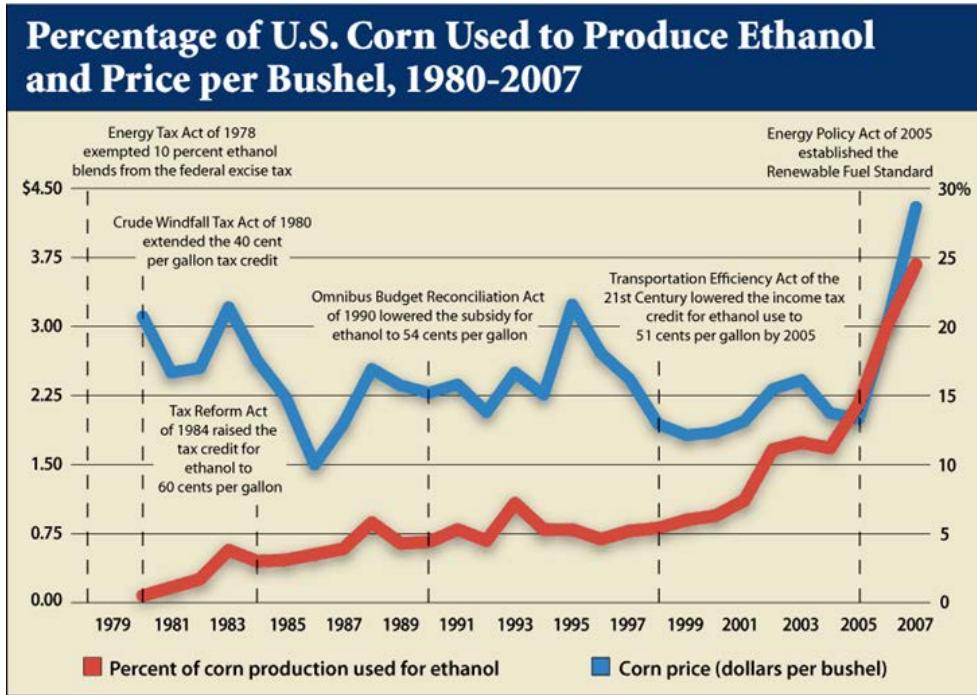


Source: U.S. Energy Information Administration (EIA)

**Figure 2**  
**Bioethanol and Biodiesel**

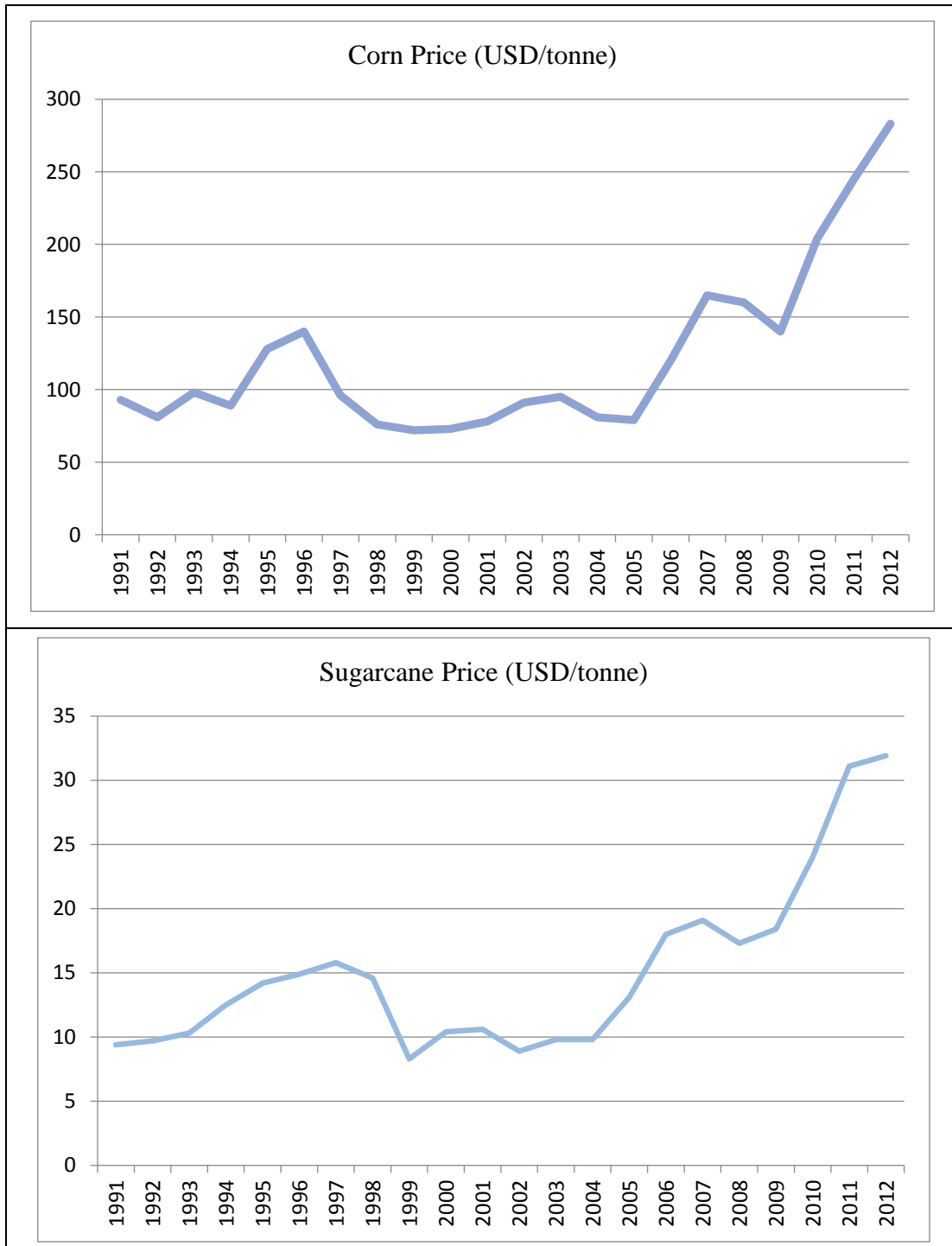


**Figure 3**  
**Percentage of US Corn to Produce Ethanol and Price per Bushel**



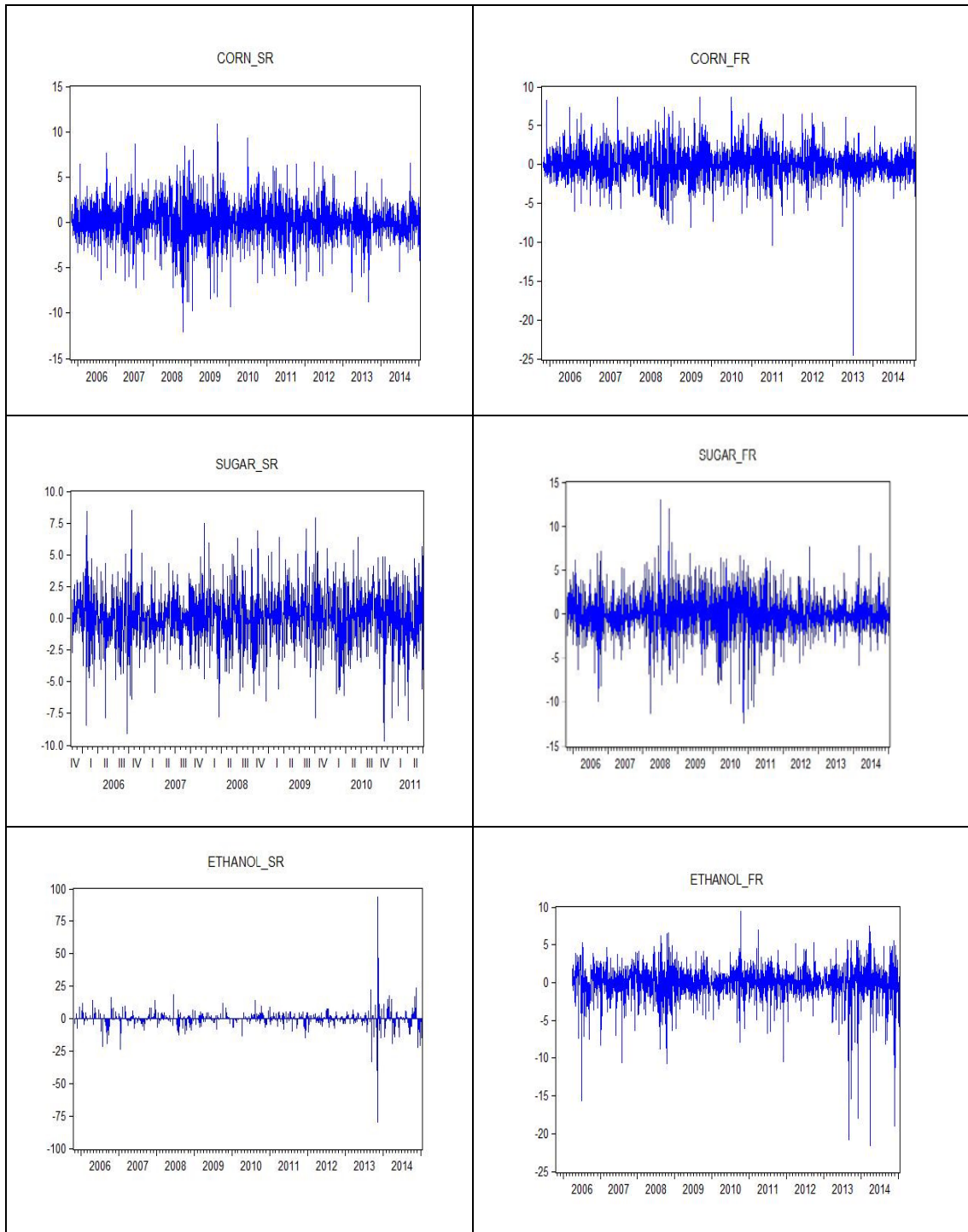
Source: United States Department of Agriculture (USDA) and U.S. Energy Information Administration (EIA)

**Figure 4**  
**Historical Prices of Corn and Sugarcane**

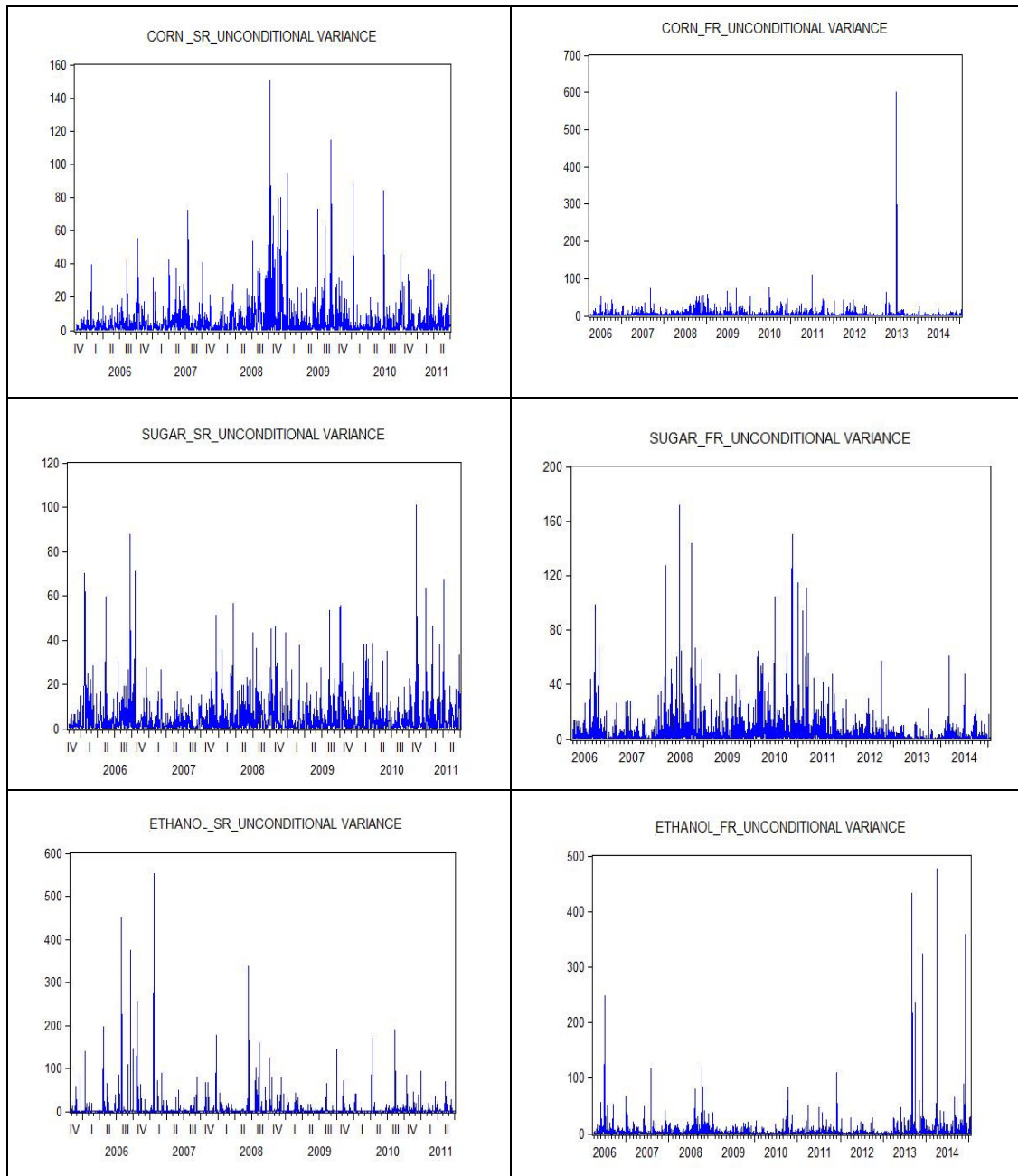


Source: FAO STAT

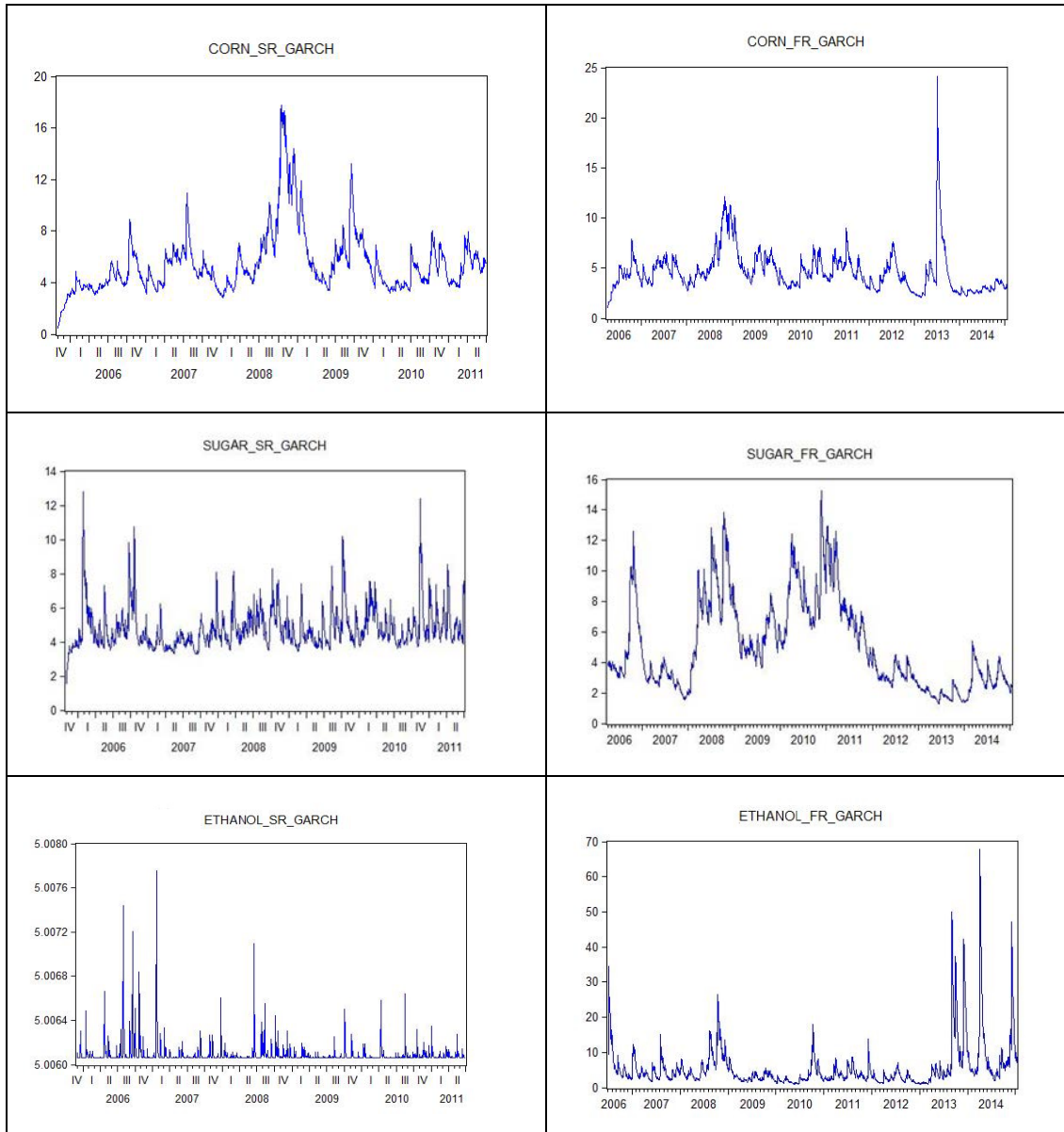
**Figure 5**  
**Corn, Sugarcane & Ethanol Spot and Futures Returns**



**Figure 6**  
**Unconditional Volatility of Corn Sugarcane & Ethanol Spot and Futures Returns**



**Figure 7**  
**Conditional volatility for Corn Sugarcane & Ethanol Spot and Futures Returns**



**Figure 8**  
**Conditional volatility for Corn & Sugarcane, Corn & Ethanol Sugarcane**  
**& Ethanol Spot and Futures Returns**

